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## Mini Review

# $J/\Psi$ (1S) and $\Psi$ (2S) Production in p-p Collisions at E=5.44 TeV

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## Abstract

I estimate the differential rapidity cross sections for  $J/\Psi$  and  $\Psi$  (2S) via pp (proton-proton) collisions at E=510 GeV. The  $J/\Psi$  is a standard charm quark and anti-charm quark,  $c$  and  $\bar{c}$  while  $\Psi$  (2S) is a mixed hybrid  $c$  meson. For the  $\Psi$  (2S) I use the mixed heavy quark hybrid theory, with states approximately 50% standard and 50% hybrid charmonium.

## Introduction

This new work on p-p collisions is based on the heavy quark state production formalism in Pb-Pb collisions at  $\sqrt{s_{pp}}$  = p-p energy = 5.02 TeV [1].

I use the standard model the for  $J/\Psi$  state and the mixed hybrid theory [2] for  $\Psi$  (2S) the state.

In section 2 heavy quark hybrid states and mixed heavy quark hybrid states are reviewed. The charm quark  $c$  is needed with a mass [3]  $m_c \simeq 1.27$  GeV.

Also, the anti-quark  $\bar{c}$  is needed. As discussed in section 2 the state  $J/\Psi$  (1S) is  $|c\bar{c}(1S)\rangle$  while state  $\Psi$  (2S) is a mixed hybrid  $c$  meson.

In section 3,  $\Psi$  production in p-p collisions is reviewed. My new work on heavy quark state production is based on the methods used in heavy quark state production in Cu-Cu and Au-Au collisions at  $\sqrt{s_{pp}} = 200$  GeV[4] which used the color octet model [5-7]. Prior to the article [?]  $\Psi$  (2S) and  $\Psi$ (3S) suppression in p-Pb collisions with E =  $\sqrt{s_{pp}} = 5.02$  TeV was

estimated [8] and reviewed [9]. Also, the ALICE collaboration studied  $J/\Psi$  production via Xe-Xe collisions at  $\sqrt{s_{NN}} = 5.44$  TeV [10].

## Normal and mixed Charmonium States

The starting point of the method of QCD sum rules [11] is the correlator

$$\Pi^A(x) = \langle T[J_A(x)J_A(0)] \rangle, \quad (1)$$

With  $| \rangle$  the vacuum state and the current  $J_A(x)$  creates the states with quantum numbers A.

With  $c$ ,  $\bar{c}$  and  $g$  a charm quark, an anti-charm quark, and a gluon.

For the normal charmonium state  $J/\Psi$  (1S)

$$J_{c\bar{c}} = J_{\bar{c}c}, \quad (2)$$

while the mixed hybrid charmonium state  $\Psi$  (2S)  $J_c$  is

$$J_{c\bar{c}g} \simeq -fJ_{\bar{c}c} + \sqrt{1-f^2}J_{c\bar{c}g}, \quad (3)$$

where  $f = 2$ .



Note that  $J_{c\bar{c}}$  creates a normal charmonium state  $J/\Psi$  (1S) and  $J_{c\bar{c}g}$  creates a hybrid state  $\Psi$  (2S).

### Differential rapidity cross sections for $J/\Psi$ (1S) Production at E= 510 GeV

In the present work I use the theory described in detail in Ref [12] with applications to BNL-RHIC, LHC and Fermilab, based on the octet model [5-7] for pp production of heavy quark states; and used for studies of pp collisions for Upsilon production at forward rapidities [13] and for heavy quark production at 7 TeV [14] and 8 TeV [15]. This calculation is motivated by the report of preliminary data for  $J/\Psi$ ,  $\Psi$  (2S) production via pp collisions at 510 GeV by the PHENIX Collaboration [16].

For helicity  $\lambda = 0$ , the differential rapidity cross section is given by [12]

$$\frac{d\sigma_{pp \rightarrow \Phi(\lambda=0)}}{dy} = A_{\Phi} \frac{1}{x(y)} f_g(x(y), 2m) f_g(a/x(y), 2m) \frac{dx}{dy}, \tag{4}$$

with with  $a = 4m^2/s = 3.46 \times 10^{-5}$ ,  $s = E^2$ ,  $E = 510$  GeV,  $m = 1.5$  GeV (for charm quark) and [12]  $A_{\Phi} = \frac{5\pi^3 \alpha_s^2}{288m^3 s} \langle O_8^{\Phi}(1S_0) \rangle = 3.1 \times 10^{-4}$  nb.  $X(y)$  and  $\frac{dx}{dy}$  are given by (there was a typo in the numerator of  $\frac{dx(y)}{dy}$ , within Ref [12])

$$x(y) = 0.5 \left[ \frac{m}{510} (\exp y - \exp(-y)) + \sqrt{\left(\frac{m}{510} (\exp y - \exp(-y))\right)^2 + 4a} \right]$$

$$\frac{dx(y)}{dy} = \frac{m}{1020} (\exp y + \exp(-y)) \left[ 1 + \frac{\frac{m}{510} (\exp y - \exp(-y))}{\sqrt{\left(\frac{m}{510} (\exp y - \exp(-y))\right)^2 + 4a}} \right]. \tag{5}$$

The gluonic distribution function  $f_g(x)$ , for  $\sqrt{s} = E = 510$  GeV [12], is

$$f_g(x) \simeq 1334.21 - 67056.5x + 887962.0x^2. \tag{6}$$

From Eqs(4,2,6) the differential rapidity cross sections for  $J/\Psi$  (1S) production via 510 GeV p-p collisions with the standard theory [3] are shown in the figure below.

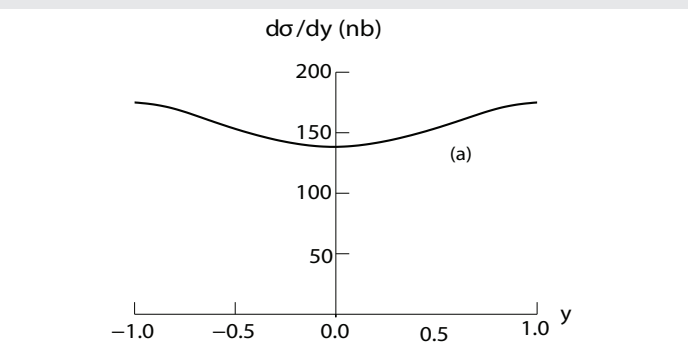


Figure 1:  $d\sigma/dy$  for E=510 GeV p-p collisions with  $\lambda = 0$  producing (a)  $J/\Psi$  (1S) with a standard  $c\bar{c}$  model.

## Conclusion

I have calculated the differential cross sections for pp collisions at 510 GeV for  $J/\Psi$  (1S) production with the standard  $|c\bar{c}(1S)\rangle$  model. As shown in the figure,  $\frac{d\sigma_{pp \rightarrow J/\Psi(1S)}}{dy} \simeq 150$  nb.

The cross-section for  $J/\Psi$  (1S) production in the standard model has been found in pp collision experiments at 200GeV [12].

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